# Earth Observation <br> Mission CFI Software 

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## 1 SCOPE

This document describes in detail the time references and formats, reference frames, parameters, models, and units that will be used by the Earth Observation Mission CFI Software. The description sometimes goes beyond the CFI-needed information, when deemed necessary for the sake of a correct explanation.

All topics treated along the document are applicable to the following CFI libraries:

- EO_DATA_HANDLING
- EO_LIB
- EO_ORBIT
- EO_POINTING
- EO_VISIBILITY

The present document covers the different LEO satellite missions considered in the frame of the ESA Earth Observation Programme.

## 2 ACRONYMS AND NOMENCLATURE

### 2.1 Acronyms

| ADM | Atmospheric Dynamics Mission |
| :---: | :---: |
| ANX | Ascending Node Crossing |
| AOCS | Attitude and Orbit Control Sub-system |
| CFI | Customer Furnished Item |
| DORIS | Doppler Orbitography and Radio positioning Integrated by Satellite |
| ESA | European Space Agency |
| ESTEC | European Space Technology and Research Centre |
| EO | Earth Observation |
| EOCFI | Earth Observation CFI Software |
| FK4 | Fourth Fundamental Catalogue |
| FK5 | Fifth Fundamental Catalogue |
| GOCE | Gravity Field and Steady-state Ocean Circulation Mission |
| GPS | Global Positioning System |
| IAU | International Astronomical Union |
| IERS | International Earth Rotation Service |
| IRF | Instrument Reference Frame |
| IRM | IERS Reference Meridian |
| IRP | IERS Reference Pole |
| ITRF | IERS Terrestrial Reference Frame |
| JD | Julian Day |



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## 3 APPLICABLE AND REFERENCE DOCUMENTS

### 3.1 Applicable Documents

### 3.2 Reference Documents

| ALMAN95 | The Astronomical Almanac for the year 1995. |
| :---: | :---: |
| ALMAN05 | The Astronomical Almanac for the year 2005. |
| BOWRING | Method of Bowring. NGT Geodesia 93-7. P 333-335. 1993. |
| CELES | www.celestrak.com |
| FLANDERN | Low-precision formulae for planetary positions. Astrophysical Journal Supplement Series: 41. P 391-411. T.C.Van Flandern, K.F. Pulkkinen. November 1979. |
| GREEN | Spherical Astronomy. Green, R.M. 1985 |
| HEISKANEN | Physical Geodesy. Weikko A. Heiskanen, Helmut Moritz. Graz 1987. |
| IERS_SUPL | Explanatory Supplement to IERS Bulletins A and B. International Earth Rotation Service (IERS). March 1995. |
| KLINKRAD | Semi-Analytical Theory for Precise Single Orbit Predictions of ERS-1. ER-RP-ESA-SY-004. H.K. Klinkrad (ESA/ESTEC/WMM). Issue 1.0. 28/06/87. |
| LIU_ALFORD | Semianalytic Theory for a Close-Earth Artificial Satellite. Journals of Guidance and Control Vol. 3, No 4. J.J.F. Liu and R.L. Alford. July-August 1980. |
| MCD_SP | Earth Observation Mission CFI Software MISSION SPECIFIC CUSTOMIZATIONS. EO-MA-DMS-GS-018. Issue 1.0 27/10/2009 |
| OAD_TIME | OAD Standards: Time and Coordinate Systems for ESOC Flight Dynamics Operations. Orbit Attitude Division, ESOC. Issue 1. May 1994. |

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| SHOEMAKE | "Animating Rotation with Quaternions Curves", Ken Shoemake, SIGGRAPH <br> '85: Proceedings of the $12^{\text {th }}$ annual conference on Computer graphics and <br> interactive Techniques, July 1985 |
| :--- | :--- |
| STD76 | U.S. Standard Atmosphere 1976. National Oceanic and Atmosphere <br> Administration. |
| EDLEN | "Handbook of geophysics and the space environment". Adolph S. Jursa. Air <br> Force Geophysics Laboratory, 1985. |
| EO_OPS | Earth Observation OPS Commanding. <br> Link to Technical note |
| FFS | Earth Observation Mission Software File Format Specification. |

## 4 TIME REFERENCES AND MODELS

### 4.1 Time References

The time references which may be used in the context of the Earth Observation missions are listed in table:
Table 1: Earth Observation time reference definitions

| Time reference | Usage Examples |
| :--- | :--- |
| Universal Time (UT1) | Typically used as time reference for orbit state vectors. |
| Universal Time Coordinated <br> (UTC) | Typically used as time reference for all products datation. |
| International Atomic Time (TAI) | DORIS products. |
| GPS Time | Typically used by missions having a GPS receiver on-board (eg. <br> GOCE, ADM, Sentinel 1, Sentinel 2, Sentinel 3). |

The relationships between UT1, UTC and TAI are illustrated in the following figure:



Figure 1: Relationships between UT1, UTC and TAI

Universal Time (UT1) is a time reference that conforms, within a close approximation, to the mean diurnal motion of the Earth. It is determined from observations of the diurnal motions of the stars, and then corrected for the shift in the longitude of the observing stations caused by the polar motion.

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The time system generally used is the Coordinated Universal Time (UTC), previously called Greenwich Mean Time. The UTC is piece wise uniform and continuous, i.e. the time difference between UTC and TAI is equal to an integer number of seconds and is constant except for occasional jumps from inserted integer leap seconds. The leap seconds are inserted to cause UTC to follow the rotation of the Earth, which is expressed by means of the non uniform time reference Universal Time UT1.

If UT1 is predicted to lag behind UTC by more than 0.9 seconds, a leap second is inserted. The message is distributed in a Special Bulletin C by the International Earth Rotation Service (IERS).

The insertion of leap seconds is scheduled to occur with first preference at July 1st and January 1st at 00:00:00 UTC, and with second preference at April 1st and October 1st at 00:00:00 UTC.
$\Delta \mathrm{UT} 1=\mathrm{UT1}-\mathrm{UTC}$ is the increment to be applied to UTC to give UT1, expressed with a precision of 0.1 seconds, and which is broadcasted, and any change announced in a Bulletin D, by the IERS ${ }^{1}$.

DUT1 is the predicted value of $\Delta$ UT1. Predictions of UT1 - UTC daily up to ninety days, and at monthly intervals up to a year in advance, are included in a Bulletin A which is published weekly by the IERS.

International Atomic Time (TAI) represents the mean of readings of several atomic clocks, and its fundamental unit is exactly one SI second at mean sea level and is, therefore, constant and continuous.
$\Delta \mathrm{TAI}=\mathrm{TAI}-\mathrm{UTC}$ is the increment to be applied to UTC to give TAI.
GPS Time is an atomic clock time similar to but not the same as UTC time. It is synchronised to UTC but the main difference relies in the fact that GPS time does not introduce any leap second. Thus, the introduction of UTC leap second causes the GPS time and UTC time to differ by a known integer number of cumulative leap seconds; i.e. the leap seconds that have been accumulated since GPS epoch in midnight January 5, 1980.
$\Delta$ GPS $=$ TAI - GPS is the increment to be applied to GPS to give TAI, being a constant value of 19 seconds.

### 4.2 Time formats

The Julian Day (JD) is the interval of time in days and fraction of a day since 4713 BC January 1 at Greenwich noon (12:00:00).
The Modified Julian Day 2000 (MJD2000) is the interval of time in days and fraction of day since 2000 January 1 at 00:00:00.

$$
\mathrm{JD}=\text { MJD2000 }+2451544.5 \text { [decimal days] }
$$

The time format year, month, day of month, hour, minute and second follows the Gregorian calendar.

### 4.2.1 Earth Observation time formats

The time formats used with the time references proposed in section 4.1 can be one of the following:

- Processing
- Transport
- ASCII


## 1 UUT1 usually changes 1-2 ms per day

Table 2: Earth Observation time formats
$\left.\left.\begin{array}{|l|l|l|}\hline \text { Time format } & \text { Description } & \text { Usage } \\ \hline \text { Processing } & \begin{array}{l}\text { 64-bits floating point number, for } \\ \text { decimal days }\end{array} \\ \text { Internal processing, such as } \\ \text { product processing } \\ \text { sequences. Only for } \\ \text { continuous times, i.e. TAI }\end{array}\right] . \begin{array}{l}\text { Three 32-bits integer numbers for } \\ \text { Transport } \\ \text { dime values exchange seconds and microseconds }\end{array}\right\}$

[^0]| CCSDS-A with reference | Text string: <br> "RRR=yyyy-mm-ddThh:mm:ss" |
| :--- | :--- |
| CCSDS-A with <br> microseconds | Text string: <br> "yyyy-mm- ddThh:mm:ss.uuuuuu" |
| CCSDS-A with reference <br> and microseconds | Text string: <br> "RRR=yyyy-mm- <br> ddThh:mm:ss.uuuuuu" |

### 4.3 Time resolution

The time resolution is one microsecond.

### 4.4 Earth Observation On-board times

The On Board Time is the time maintained by the Spacecraft and is the time reference for all spacecraft onboard activities. Depending upon the purpose and requirements of the mission, the time format used onboard the satellite will be different. See [MCD_SP] for mission specific on-board time definitions.

## 5 REFERENCE FRAMES

The following reference frames are used in the context of Earth Observation missions:
Table 3: Earth Observation reference frames usage
\(\left.$$
\begin{array}{|l|l|}\hline \text { Reference frame } & \text { Usage Examples } \\
\hline \text { Galactic } & \begin{array}{l}\text { Star position and velocities can be given in this reference } \\
\text { frame }\end{array} \\
\hline \text { Barycentric Mean of 1950 } & \begin{array}{l}\text { Some star catalogues use this reference frame to express the } \\
\text { positions of their stars. }\end{array} \\
\hline \text { Barycentric Mean of 2000 } & \begin{array}{l}\text { The star catalogues usually use this reference frame to } \\
\text { express the positions of their stars. }\end{array} \\
\hline \text { Heliocentric Mean of 2000 } & \begin{array}{l}\text { The ephemeris of the planets are usually expressed in this } \\
\text { reference frame. }\end{array} \\
\hline \text { Geocentric Mean of 2000 } & \begin{array}{l}\text { The FOCC performs the internal calculations related to the } \\
\text { predicted and restituted orbits in this reference frame. }\end{array} \\
\hline \text { Mean of Date } & \begin{array}{l}\text { The Mean Local Solar Time is defined in this reference } \\
\text { frame. }\end{array} \\
\hline \text { True of Date } & \begin{array}{l}\text { It is the inertial reference frame used for input and output in } \\
\text { the CFI software (e.g. star positions). }\end{array} \\
\hline \text { Earth fixed } & \begin{array}{l}\text { It is the reference frame used for input and output of the } \\
\text { satellite state vector (i.e. orbit definition), and for the output } \\
\text { for geolocation in the CFI software. }\end{array} \\
\hline \text { Pseudo Earth Fixed } & \begin{array}{l}\text { It is similar to Earth Fixed but without considering polar } \\
\text { motion rotation. }\end{array} \\
\hline \text { Topocentric } & \begin{array}{l}\text { It is the local horizontal reference frame used to define a } \\
\text { looking direction. }\end{array} \\
\hline \text { Satellite Orbital } & \begin{array}{l}\text { It is a reference frame centred in the satellite and defined by } \\
\text { the satellite position and velocity. Its used as a reference for } \\
\text { the application of the selected attitude control mode. }\end{array} \\
\hline \text { Instrument Attitude } & \begin{array}{l}\text { It is used for the attitude determination. It is based on relation } \\
\text { with the Satellite Orbital frame. }\end{array}
$$ <br>
It is the reference frame that constitutes the reference for the <br>
definition of a look direction relative to the satellite (e.g. to <br>

express the pointing of an instrument).\end{array}\right\}\)| It is used for the attitude determination as well. It is based on |
| :--- |
| relation the Satellite Nominal Attitude frame or on |$|$

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### 5.1 General Reference Frames

### 5.1.1 Galactic

The galactic plane is determined by the statistical study of the galactic dynamics. In this reference frame, position are determined by a galactic latitude and longitude. The galactic latitude are taken as the angle measured from the galactic plane, while the galactic longitude are measured from the direction of the galactic centre.
In order to relate the galactic coordinates of a star to its equatorial coordinates, it is necessary to know the position of the galactic pole and the position of the galactic centre. These points have been adopted as follow, for the epoch 1950.0:

Right ascension of the Galactic pole $=12 \mathrm{~h} 49 \mathrm{~m}$.
Declination of the Galactic pole $=27^{\circ} .4$.
Galactic longitude of the north celestial pole $=123^{\circ}$ (also known as the position angle of the galactic centre)

### 5.1.2 Barycentric Mean of 1950

It is based on the star catalogue FK4 for the epoch B1950, since the directions of its axes are defined relatively to a given number of that star catalogue positions and proper motions.
The centre of this reference frame is the barycentre of the Solar System. The x-y plane coincides with the predicted mean Earth equatorial plane at the epoch B1950, and the x-axis points towards the predicted mean vernal equinox. The latter is the intersection of the mean equator plane with the mean ecliptic, and the ecliptic is the orbit of the Earth around the Sun. The z-axis points towards north.

The word mean indicates that the relatively short periodic nutations of the Earth are smoothed out in the calculation of the mean equator and equinox.

### 5.1.3 Barycentric Mean of 2000

It is based, according to the recommendations of the International Astronomical Union (IAU), on the star catalogue FK5 for the epoch J2000.0, since the directions of its axes are defined relatively to a given number of that star catalogue positions and proper motions.
The accuracy of this reference system, realized through the FK 5 star catalogue, is approximately $0.1^{\prime \prime}$.
The centre of this reference frame is the barycentre of the Solar System. The x-y plane coincides with the predicted mean Earth equatorial plane at the epoch J 2000.0 , and the x -axis points towards the predicted mean vernal equinox. The latter is the intersection of the mean equator plane with the mean ecliptic, and the ecliptic is the orbit of the Earth around the Sun. The z-axis points towards north.
The word mean indicates that the relatively short periodic nutations of the Earth are smoothed out in the calculation of the mean equator and equinox.

### 5.1.4 Heliocentric Mean of 2000

It is obtained by a parallel translation of the Barycentric Mean of 2000.0 reference frame from the barycenter of the Solar System to the centre of the Sun.
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### 5.1.5 Geocentric Mean of 2000

It is obtained by a parallel translation of the Barycentric Mean of 2000.0 reference frame from the barycenter of the Solar System to the centre of the Earth.

### 5.1.6 Mean of Date

The centre of this reference frame is the centre of the Earth. The $x-y$ plane and the $x$-axis are defined by the mean Earth equatorial plane and the mean vernal equinox of date. The expression mean of date means that the system of coordinate axes are rotated with the Earth's precession from J2000.0 to the date used as epoch. The z -axis points towards north.

The precession of the Earth is the secular effect of the gravitational attraction from the Sun and the Moon on the equatorial bulge of the Earth.

### 5.1.7 True of Date

The centre of this reference frame is the centre of the Earth. The $x-y$ plane and the $x$-axis are defined by the true Earth equatorial plane and the true vernal equinox of date. The expression true of date indicates the instantaneous Earth equatorial plane and vernal equinox. The transformation from the Mean of Date to the True of Date is the adopted model of the nutation of the Earth.

The nutation is the short periodic effect of the gravitational attraction of the Moon and, to a lesser extent, the planets on the Earth's equatorial bulge.

### 5.1.8 Pseudo Earth Fixed

It is defined the same way as Earth Fixed reference frame. The difference is that polar motion rotation is not considered in this case.

### 5.1.9 Earth Fixed

The Earth fixed reference frame in use is the IERS Terrestrial Reference Frame (ITRF).
The zero longitude or IERS Reference Meridian (IRM), as well as the IERS Reference Pole (IRP), are maintained by the International Earth Rotation Service (IERS), based on a large number of observing stations, and define the IERS Terrestrial Reference Frame (ITRF).

### 5.1.10 Topocentric

Its z-axis coincides with the normal vector to the Earth's Reference Ellipsoid, positive towards zenith. The x - y plane is the plane orthogonal to the z -axis, and the x -axis and y -axis point positive, respectively, towards east and north.

### 5.1.11 LIF (Launch Inertial Frame)

The Launch Inertial Frame (LIF) is an Coordinate System whose Z axis and XY plane are the same as Z axis and XY plane of Earth Fixed Coordinate System. It is a user defined Coordinate System as the user needs to provide a longitude and a UTC time to define it. More precisely, $\mathrm{X}, \mathrm{Y}$ and Z axes are defined as follows:

- X axis: is in the equatorial plane and points where a given user defined meridian was at a given user defined UTC time. The meridian is defined by the user specifying the value of the corresponding longitude (note that, if longitude $=0$, the reference is the Greenwich meridian)
- $\quad \mathrm{Z}$ axis: is in the direction of the angular velocity of the Earth (= towards North Pole)
- Y axis: complete the right-handed coordinate system


### 5.2 Satellite Reference Frames

A sequential combination of four levels of reference frames are used for attitude determination:

- Satellite Orbital frame (SOF)
- Satellite Nominal reference frame (SNRF)
- Satellite reference frame (SRF)
- Instrument reference frame (IRF)


### 5.2.1 Satellite Orbital frame

The Satellite Orbit frame (SOF) is a reference frame completely determined by the Satellite position and velocity, and is used as basis for the computation of the other satellite reference frames.
The SOF is centred on the satellite and is defined by the Xs, Ys and Zs axes, which are specified relatively to the reference inertial reference frame, namely the True of Date:

- the Zs axis points along the radial satellite direction vector, positive from the centre of the TOD reference frame towards the satellite
- the Ys axis points along the transversal direction vector within the osculating orbital plane (i.e the plane defined by the position and velocity vectors of the satellite), orthogonal to the Zs axis and opposed to the direction of the orbital motion of the satellite
- the Xs axis points towards the out-of-plane direction vector completing the right hand reference frame.

$$
\vec{Z}=\frac{\vec{r}}{|\vec{r}|} \quad \vec{X}=\frac{\vec{r} \wedge \vec{v}}{|\vec{r} \wedge \vec{v}|} \quad \vec{Y}=\vec{Z} \wedge \vec{X}
$$

where $\overline{\mathrm{X}}, \overline{\mathrm{Y}}$ and $\overline{\mathrm{Z}}$ are the unitary direction vectors in the (Xs, Ys, Zs) axes, and $\vec{r}$ and $\vec{v}$ are the position and velocity vectors of the satellite expressed in the inertial reference frame.
The following figure depicts the Satellite Orbital frame:


Figure 2: Satellite Orbital Frame

### 5.2.2 Satellite Nominal reference frame

The Satellite Nominal reference frame (SNRF) is an ideal reference frame, typically determined by an attitude mode (i.e. a model, or law, that establishes the reference frame axis definition).

The complete list of attitude modes with the specification of the axis definition is provided in section 8.1, including the following examples:

- Local Normal Pointing attitude (LNP)
- the z -axis is chosen in the direction of the satellite's zenith
- the x -axis is defined in the direction of the satellite's inertial velocity vector (in True of Date)
- Yaw Steering Mode attitude (YSM)
- the z -axis is chosen in the direction of the satellite's zenith
- the x -axis is defined in the direction of the cross product of the z -axis and the satellite's velocity vector in the Earth Fixed CS


### 5.2.3 Satellite reference frame

The Satellite reference frame (SRF) corresponds to the satellite actual (measured) attitude frame. It could be considered as the result of three consecutive rotations of the SNRF over three angles called mispointing angles. The time derivative of those mispointing angles are called mispointing rates.
In practice, the SRF can be determined in several ways, for example:

- with three consecutive rotations of the SNRF over three user-defined angles (mispointing angles);
- with a user-provided misalignment matrix between SNRF and SRF;
- modulating the misalignment angles with biases and harmonics (provided by the user);
- reading attitude angles (or quaternions) from a file.
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### 5.2.4 Instrument reference frame

The Instrument reference frame (IRF) is a reference frame based on the attitude of a specific satellite instrument. In case multiple satellite instruments are being considered, a separate IRF instance should be create for each instrument. The IRF determines the location (i.e. an offset from the center of SRF) and looking direction for the instrument.

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### 5.3 General Reference Frames Transformations

The following picture identifies the general reference frames transformations that are relevant for the Earth Observation missions.


> Reference frames: $\begin{array}{ll}\text { GALACTIC } & =\text { Galactic CS (see section 5.1.1) } \\ \text { BM1950 } & =\text { Barycentric Mean of } 1950.0 \text { (see section 5.1.2) } \\ \text { BM2000 } & \text { = Barycentric Mean of } 2000.0 \text { (see section 5.1.3) } \\ \text { HM2000 } & \text { = Heliocentric Mean of } 2000.0 \text { (see section 5.1.4) } \\ \text { GM2000 } & \text { = Geocentric Mean of } 2000.0 \text { (see section 5.1.5) } \\ \text { MoD } & \text { = Mean of Date (see section 5.1.6) } \\ \text { ToD } & \text { = True of Date (see section 5.1.7) } \\ \text { PEF } & \text { = Pseudo Earth Fixed (see section 5.1.8) } \\ \text { EF } & \text { = Earth Fixed (see section 5.1.9) } \\ \text { LIF } & \text { = Launch Inertial Frame (see section 5.1.11) }\end{array}$

Transfromations:
TR1 = Galactic to Barycentric Mean of 1950 (see section 5.3.1)
TR2 = Barycentric 1950 to Barycentric 2000 (see section 5.3.2)
TR3 $=$ Solar system barycentre to Earth centre translation (see section 5.3.3)
TR3' = Sun centre to Earth centre translation (see section 5.3.4)
TR4 = Precession (see section 5.3.5)
TR5 $=$ Nutation (see section 5.3.6)
TR6 $=$ Earth rotation + nutation term (see section 5.3.7)
TR7 = Polar motion rotation (see section 5.3.8)
TR8 = Earth rotation
Figure 3: General Reference Frames Transformations

Those transformation are described in the following sections.
Note that whenever a transformation is expressed as a sequence of rotations, the following expressions apply (the angle $w$ is regarded positive):
$R_{X}(w)=\left[\begin{array}{ccc}1 & 0 & 0 \\ 0 & \cos w & \sin w \\ 0 & -\sin w & \cos w\end{array}\right] R_{Y}(w)=\left[\begin{array}{ccc}\cos w & 0 & -\sin w \\ 0 & 1 & 0 \\ \sin w & 0 & \cos w\end{array}\right] R_{Z}(w)=\left[\begin{array}{ccc}\cos w & \sin w & 0 \\ -\sin w & \cos w & 0 \\ 0 & 0 & 1\end{array}\right]$

### 5.3.1 Galactic to Barycentric Mean of 1950

The following picture represents the galactic and the equatorial coordinate systems. The relationship between both systems are given by the equatorial coordinates of the galactic pole for the epoch 1950 and for by the position of the galactic centre.


P North Pole (for epoch B1950)
G Galactic North Pole
C Galactic centre
$\delta_{g}$ Declination of the Galactic pole $=12^{\mathrm{h}} 49^{\mathrm{m}}$
$\alpha_{g}$ Right Ascension of the Galactic pole $=27.4^{\circ}$
$\theta$ Position of the galactic centre $=123^{\circ}$
$l$ Galactic longitude of the point X
$b$ Galactic latitude of the point X

Figure 4: Galactic and Equatorial coordinates

In the figure, considering the spheric triangle GPX, the relationship between the galactic and equatorial coordinates can be established (see GREEN for further details)

$$
\begin{aligned}
& \cos \mathrm{b} \sin (\theta-\mathrm{l})=\cos \delta \sin \left(\alpha-\alpha_{g}\right) \\
& \cos \mathrm{b} \cos (\theta-\mathrm{l})=\cos \delta_{g} \sin \delta-\sin \delta_{g} \cos \delta \cos \left(\alpha-\alpha_{g}\right)
\end{aligned}
$$

Taking into account the relations between spherical and cartesian coordinates, it is easy to derive the rotation matrix from Galactic to Barycentric B1950.0:

$$
R_{(\text {galactic } \rightarrow \text { B1950.0) }}=\left[\begin{array}{ccc}
-0,06698874 & 0,49272847 & -0,86760081 \\
-0,8727557659 & -0,45034696 & -0,1883746 \\
-0,4835389146 & 0,74458463 & 0,46019978
\end{array}\right]
$$

### 5.3.2 Barycentric Mean of 1950.0 to Barycentric Mean of 2000

The transformation from barycentric B1950.0 to barycentric J2000 includes the following processes:

1. Removal of the terms of elliptic aberration.
2. Rotation to the dynamical equinox of B1950.0
3. Correcting the proper motions for the equinox motion and the change in the value of precession
4. Changing from tropical to Julian centuries for the time scale of proper motions
5. Updating of positions to the epoch of J2000
6. Precession of positions and proper motions from B1950.0 to J2000.

For further details about this transformation, refer to:

- ALMAN05(B32)
- Astronomical and Astrophysical Journal 128, 263-267 (1983)


### 5.3.3 Barycentric Mean of 2000 to Geocentric Mean of 2000

The transformation from the Barycentric Mean of 2000 to the Geocentric Mean of 2000 reference frame is calculated with the following expressions


P North Pole (for epoch B1950)
G Galactic North Pole
C Galactic centre
$\delta_{g}$ Declination of the Galactic pole $=12^{\mathrm{h}} 49^{\mathrm{m}}$
$\alpha_{g}$ Right Ascension of the Galactic pole $=27.4^{\circ}$
$\theta$ Position of the galactic centre $=123^{\circ}$
$l$ Galactic longitude of the point X
$b$ Galactic latitude of the point X

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):

$$
\begin{aligned}
& \overline{\mathrm{r}}_{\mathrm{E}}=\overline{\mathrm{r}}_{\mathrm{B}}-\overline{\mathrm{r}}_{\mathrm{B}, \text { Earth }} \\
& \overline{\mathrm{v}}_{\mathrm{E}}=\overline{\mathrm{v}}_{\mathrm{B}}-\overline{\mathrm{v}}_{\mathrm{B}, \mathrm{Earth}}
\end{aligned}
$$

where $\overrightarrow{r_{E}}$ and $\overrightarrow{v_{E}}$ are the position and velocity vectors in the Geocentric Mean of 2000 reference frame, $\overrightarrow{r_{B}}$ and $\overrightarrow{v_{B}}$ are the position and velocity vectors in the Barycentric Mean of 2000 reference frame, and $\vec{r}_{B, E a r t h}$ and $\vec{v}_{B, E a r t h}$ are the position and velocity vectors of the Earth in the Barycentric Mean of 2000 reference frame.
$\vec{r}_{B, \text { Earth }}$ and $\vec{v}_{B, E a r t h}$ are calculated according to BOWRING reference.

Figure 5: Transformations between BM2000, HM2000 and GM2000 reference frames

### 5.3.4 Heliocentric Mean of 2000 to Geocentric Mean of 2000

The transformation from the Heliocentric Mean of 2000 to the Geocentric Mean of 2000 reference frame is calculated with the following expressions (


## Figure 5



Figure 5):

$$
\begin{aligned}
& \overline{\mathrm{r}}_{\mathrm{E}}=\overline{\mathrm{r}}_{\mathrm{H}}-\overline{\mathrm{r}}_{\mathrm{H}, \text { Earth }} \\
& \overline{\mathrm{v}}_{\mathrm{E}}=\overline{\mathrm{v}}_{\mathrm{H}}-\overline{\mathrm{v}}_{\mathrm{H}, \text { Earth }}
\end{aligned}
$$

where $\vec{r}_{E}$ and $\vec{v}_{E}$ are the position and velocity vectors in the Geocentric Mean of 2000 reference frame, $\vec{r}_{H}$ and $\vec{v}_{H}$ are the position and velocity vectors in the Heliocentric Mean of 2000 reference frame, and $\vec{r}_{H, E a r t h}$ and $\vec{v}_{H, E a r t h}$ are the position and velocity vectors of the Earth in the Heliocentric Mean of 2000 reference frame.
$\vec{r}_{H, E a r t h}$ and $\vec{v}_{H, E \text { Earth }}$ are calculated according to BOWRING reference.

### 5.3.5 Geocentric Mean of 2000 to Mean of Date

The transformation from the Geocentric Mean of 2000 to the Mean of Date reference frame is performed with the following expression



Figure 6):

$$
\overline{\mathrm{r}}_{\mathrm{m}}=\mathrm{R}_{\mathrm{z}}\left(-\frac{\pi}{2}-\mathrm{z}\right) \mathrm{R}_{\mathrm{x}}(\theta) \mathrm{R}_{\mathrm{z}}\left(\frac{\pi}{2}-\zeta\right) \overline{\mathrm{r}}_{\mathrm{J} 2000}
$$

where $\vec{r}_{m}$ and $\vec{r}_{J 2000}$ are the position vector in the Mean of Date and the Mean of 2000 reference frame, respectively.

The rotation angles of the precession model are calculated as follows (OAD_TIME reference):

Code:

$$
\begin{aligned}
& \xi=0.6406161 T+0.0000839 T^{2}+0.0000050 T^{3}[\mathrm{deg}] z \\
&=0.6406161 T+0.0003041 T^{2}+0.0000051 T^{3}[\mathrm{deg}] \\
& \vartheta=0.5567530 T-0.0001185 T^{2}-0.0000116 T^{3}[\mathrm{deg}]
\end{aligned}
$$

where T is the TDB time expressed in the Julian centuries format ( 1 Julian century $=36525$ days).
However, the precession motion is so slow that the UTC time can be used instead of the TDB time, and therefore T can be calculated from t , the UTC time expressed in the MJD2000 format, with the following expression:

$$
\mathrm{T}=(\mathrm{t}-0.5) / 36525 \text { [Julian centuries] }
$$



Figure 6: Transformation between GM200 and MoD reference frames

### 5.3.6 Mean of Date to True of Date

The transformation from the Mean of Date to the True of Date reference frame is performed with the following expression


7):

$$
\overline{\mathrm{r}}_{\mathrm{t}}=\mathrm{R}_{\mathrm{z}}(-\delta \mu) \mathrm{R}_{\mathrm{x}}(-\delta \varepsilon) \mathrm{R}_{\mathrm{y}}(\delta v) \overline{\mathrm{r}}_{\mathrm{m}}
$$

where $\vec{r}_{t}$ and $\vec{r}_{m}$ are, respectively, the position vector in the True of Date and the Mean of Date reference frame.

The rotation angles of the simplified nutation model are calculated with (OAD_TIME reference):

$$
\begin{gathered}
\delta \mu=\delta \psi \cos \varepsilon \\
\delta v=\delta \psi \sin \varepsilon
\end{gathered}
$$

where $\varepsilon$ is the obliquity of the ecliptic at the epoch J2000:

$$
\varepsilon=23.439291[\mathrm{deg}]
$$

and $\delta \varepsilon$ and $\delta \psi$ is expressed by the Wahr model taking only the nine largest terms, and using UT1 instead of TDB as the time reference.


Figure 7: Transformation between MoD and ToD reference frames

Code:

### 5.3.7 True of Date to Pseudo Earth Fixed

The transformation from the True of Date to the Pseudo Earth fixed reference frame is performed with the
$\qquad$
following expression (


## Figure 8

Figure 8):

$$
\vec{r}_{p e}=R_{z}(H) \vec{r}_{t}
$$

where $\vec{r}_{p e}$ and $\vec{r}_{t}$ are, respectively, the position vector in the Pseudo Earth fixed and in the True of Date reference frames.

The Earth rotation angle $\boldsymbol{H}$ is the sum of the Greenwich sidereal angle and a small term from the nutation in the longitude of the equinox.

The Greenwich sidereal angle moves with the daily rotation of the Earth and is calculated with the Newcomb's formula according to international conventions as a third order polynomial, although the third order term will be neglected in our calculations.
The nutation term is calculated with the simplified nutation model (see section 5.1.7).

$$
\begin{aligned}
& H=G+\delta \mu \\
& G=99.96779469+360.9856473662860 T+0.29079 \times 10^{-12} T^{2}[d e g]
\end{aligned}
$$

where T is the UT1 time expressed in the MJD2000 format.
Note that the transformation from the Mean of Date to the Pseudo Earth fixed reference frame can be performed in one step being the $\delta \mu$ rotation term cancelled out:

$$
\vec{r}_{p e}=R_{z}(G) R_{x}(-\delta \varepsilon) R_{y}(\delta v) \vec{r}_{q m}
$$



Figure 8: Transformation between ToD and PEF reference frames

### 5.3.8 Pseudo Earth Fixed to Earth Fixed

The transformation from the Pseudo Earth Fixed to the Earth fixed reference frame is performed with the following expression (Figure 9Figure 9):

$$
\vec{r}_{E F}=R_{y}(-X) R_{x}(-Y) \vec{r}_{P E F}
$$

where $\vec{r}_{E F}$ and $\vec{r}_{P E F}$ are, respectively, the position vector in the Earth fixed and in the Pseudo Earth Fixed reference frames; X and Y are the polar motion parameters (measured and predicted by the IERS).


Figure 9: Transformation between PEF and EF reference frames

### 5.4 Satellite Reference Frames Transformations

There is not a general rule for transforming from one satellite reference frame to another. The attitude computation provides the transformation matrix from the satellite frame to an inertial reference frame. The following picture identifies the CFI-specific reference frames transformations that are relevant for the Earth Observation missions:


IRF = Inertial Reference Frame SRF, SRF'= Satellite/Instrument Reference Frames


Figure 10: CFI-specific Reference Frames Transformations

## 6 ORBIT CHARACTERISATION

### 6.1 Orbit Definition

### 6.1.1 Sun-synchronous Orbit

The orbit is Sun-synchronous when the rate of change of the mean right ascension of the ascending node coincides with the motion of the mean Sun:

$$
\dot{\Omega}=\dot{\overline{\mathrm{L}}}_{\text {sun }}
$$

which implies that the MLST of the ascending node is also constant. Its behaviour is graphically presented

a) Sun-synchronous orbit

b) Quasi Sun-synchronous orbit
in
Figure

a) Sun-synchronous orbit

14 (a).

a) Sun-synchronous orbit

b) Quasi Sun-synchronous orbit

Figure 11: Sun-synchronous and quasi Sun-synchronous orbits descriptions

### 6.1.2 Quasi Sun-synchronous Orbit

The orbit is quasi Sun-synchronous when the rate of change of the mean right ascension of the ascending node is shifted from the motion of the mean Sun by a constant drift. It implies that the orbit line of nodes moves backward/forward with respect to the Sun-Earth LOS. The condition can be expressed mathematically in the following way:

$$
\dot{\Omega}=\dot{\overline{\mathrm{L}}}_{\mathrm{sun}}+\mathrm{MLST}_{\mathrm{drift}}
$$

The behaviour of a quasi Sun-synchronous orbit compared to that of a Sun-synchronous orbit is presented in

a) Sun-synchronous orbit

b) Quasi Sun-synchronous orbit


11
a) Sun-synchronous orbit

b) Quasi Sun-synchronous orbit

Figure 11 (b).

### 6.1.3 Geo-synchronous Orbit

The orbit is Geo-synchronous when the ground track in the Earth Fixed reference frame repeats precisely after a constant integer number of orbits.

### 6.2 Orbit Types

### 6.2.1 Reference Orbit

The reference orbit consists of a scenario file, containing orbit information per repeat cycle change, i.e. the position and velocity vectors expressed in the Earth fixed reference frame, corresponding to the ascending node of that orbit and its associated time.

This state vector of the ascending node is calculated using the satellite-specific propagation mode, and imposing the conditions pertained the particular orbit definition.

### 6.2.2 Predicted Orbit

The predicted orbit consists of a set of satellite Cartesian state vectors that allow the computation of state vectors in the future with respect to the time in which the set has been generated.

### 6.2.3 Restituted Orbit

The restituted orbit consists of a set of consolidated satellite Cartesian state vectors that allow the computation of state vectors in the past with respect to the time in which the set has been generated.

### 6.2.4 TLE Orbit

The TLE orbit consists of two 69-character lines of data. The TLE contains mean keplerian elements for a given epoch (More info about TLE format can be found in CELES).

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### 6.3 Orbit Propagation Definition

To calculate the state vector at any point in the orbit, it is sufficient to have the orbital data (a state vector, or keplerian elements) at a given time, and then propagate that initial state vector to the required time using an orbit propagation model.

That initial orbital data can come from different sources (see section 6.2) and depending on the type of orbit and the satellite mission, there are different requirements on the accuracy of the position and velocity vectors of that initial state.

### 6.4 Orbit Propagation Models

The propagation models must incorporate an initialisation mode. It basically starts with:

- a TLE providing the mean keplerian elements at a given epoch.
- an initial cartesian state vector expressed in the Earth fixed reference frame at a given time, supplied externally (see section 6.2), to calculate the time and the state vector of the true ascending node in the Earth fixed reference frame (i.e. $\mathrm{z}_{\mathrm{AN}}=0$ and $\dot{\mathrm{z}}_{\mathrm{AN}}>0$ ).
The initialisation mode implements an iterative algorithm which is based upon a propagation mode.


### 6.4.1 Mean Keplerian Orbit Propagator

### 6.4.1.1 Simulation mode

The simulation mode is one of reduced accuracy. In this case only the zonal (i.e. latitude independent) of the geoid $\mathrm{J}_{2}, \mathrm{~J}_{2}{ }^{2}, \mathrm{~J}_{3}$ and $\mathrm{J}_{4}$ are used to calculate the secular perturbations of the mean ${ }^{4}$ Kepler elements, and the zonal harmonic J 2 is used to calculate the short periodic perturbations to transform the mean Kepler elements to the osculating Kepler elements.
This mode is based on the equations derived in LIU_ALFORD reference.

### 6.4.2 Precise Orbit Propagator

This model consists on a numerical propagator that integrates the movement equations using a Runge-Kutta algorithm of 8th order. This propagator is expected to produce more precise results than the other models. The main characteristics of the model are:

| Characteristics |  |
| :--- | :--- |
| Central Body | Earth |
| Integrator algorithm | Runge-Kutta 8 with a fixed <br> integrator step defined by the user. |
| Perturbation models | - Gravity <br> - Atmosphere <br> - Third Body - Sun <br> - Third Body - Moon <br> - Solar Radiation Pressure |

[^1]| Gravity Model <br> Gravity Model Coefficients <br> (Zonals x Tesserals) | EGM-96 |
| :--- | :--- |
| Atmosphere model | MSIS-E-90 |
| Solar Activity | Constant user-defined value |
| Geomagnetic Activities | Constant user-defined value |
| Sun Ephemerides | Analytical |
| Moon Ephemerides | Analytical |
| Aerodynamic Drag - Area | Constant user-defined value |
| Aerodynamic Drag - Drag <br> Coeffcient (CD) | Constant user-defined value |
| Solar Radiation Pressure - Area | Constant user-defined value |
| Solar Radiation Pressure - SRP <br> Coeffcient (Cr) | Constant user-defined value |

### 6.4.3 TLE Propagator

This model propagates the state vector using the NASA/NORAD "two line elements" and the SGP4 propagation model. SGP4 algorithm was designed by the NASA/NORAD for near Earth Satellites (nodal period less than 225 minutes). The SGP4 theory uses an Earth gravitational field through zonal terms J2, J3 and J4 and a power density function for the atmospheric model (assuming a non-rotating spherical model).

## 7 PARAMETERS

### 7.1 Orbit Parameters

### 7.1.1 Cartesian State Vector

It comprises the cartesian components of the position $\vec{r}_{S C}$, velocity $\vec{v}_{S C}$ and acceleration $\vec{a}_{S C}$ vectors of the satellite expressed in a specified reference frame (typically the Earth fixed reference frame) at a given epoch.

### 7.1.2 Orbit Radius, Velocity Magnitude and Components

The satellite orbit radius is the module of the satellite position vector $\vec{r}_{S C}$ :

$$
R=\left|\vec{r}_{S C}\right|
$$

The velocity magnitude is the module of the satellite velocity vector $\vec{v}_{S C}$ :

$$
V=\left|\vec{v}_{S C}\right|
$$

The satellite velocity vector when is expressed in the True of Date reference frame can be split into two components:

- Radial component: $\vec{v}_{r}=\vec{v}_{S C} \cdot \vec{Z}$
- Transversal component: $\vec{v}_{t}=-\vec{v}_{S C} \cdot \vec{Y}$
where $\vec{Y}$ and $\vec{Z}$ are the direction vectors of the Satellite Reference frame (see section 5.2.1).


### 7.1.3 Osculating Kepler State Vector

The osculating Kepler elements are related to the cartesian state vector, at the corresponding epoch, expressed in the True of Date reference frame.

The six Kepler elements are:

- Semi-major axis (a)
- Eccentricity (e)
- Inclination (i)
- Argument of perigee $(\omega)$
- Mean anomaly (M)
- Right ascension of the ascending node $(\Omega)$

Other auxiliary elements are:

- Eccentric anomaly (E)
- True anomaly (v)
- True latitude ( $\alpha$ )

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- Mean latitude $(\beta)$

The relationships between these auxiliary elements and the six Kepler elements are:

$$
\begin{aligned}
& \tan \frac{\mathrm{E}}{2}=\sqrt{\frac{1-\mathrm{e}}{1+\mathrm{e}}} \tan \frac{\mathrm{v}}{2} \\
& \mathrm{M}=\mathrm{E}-\mathrm{e} \sin \mathrm{E} \text { (Kepler's equation) } \\
& \alpha=\omega+v \\
& \beta=\omega+\mathrm{M}
\end{aligned}
$$

### 7.1.4 Mean Kepler State Vector

The osculating six Kepler elements in the True of Date reference frame can be averaged with respect to the mean anomaly over $2 \pi$, to obtain the mean Kepler elements:

$$
\overline{\mathrm{a}}, \overline{\mathrm{e}}, \overline{\mathrm{i}}, \bar{\omega}, \bar{\Omega}, \overline{\mathrm{M}}
$$

### 7.1.5 Equinoctial State Vector

The osculating Kepler elements are usually replaced by the equivalent osculating equinoctial elements for quasi-equatorial and quasi-circular orbits:
$\mathrm{x}_{1}=\mathrm{a}$
$\mathrm{x}_{2}=\mathrm{e}_{\mathrm{x}}=\mathrm{e} \cos (\Omega+\omega)$
$\mathrm{x}_{3}=\mathrm{e}_{\mathrm{y}}=\mathrm{e} \sin (\Omega+\omega)$
$\mathrm{x}_{4}=\mathrm{i}_{\mathrm{x}}=+2 \sin (\mathrm{i} / 2) \sin (\Omega)$
$\mathrm{x}_{5}=\mathrm{i}_{\mathrm{y}}=-2 \sin (\mathrm{i} / 2) \cos (\Omega)$
$\mathrm{x}_{6}=\Omega+\omega+\mathrm{M}$

### 7.1.6 Ascending Node, Ascending Node Time, Nodal Period, Absolute Orbit Number

The ascending node of an orbit is the intersection of that orbit, when the satellite goes from the southern to the northern hemisphere, with the $\mathrm{x}-\mathrm{y}$ plane of the Earth fixed reference frame.
The ANX time is the UTC time of that ascending node.
The relative time with respect to the ANX time is the time elapsed since that ascending node till the current position within the orbit.
The nodal period of an orbit is the interval of time between two consecutive ascending nodes.

The Launch orbit from the launch site is regarded as absolute orbit number zero. From then on, each time a new ascending node is crossed the absolute orbit number is incremented by one.

Note: any orbital angle calculated with respect to planes different from ToD or EF is inconsistent with the calculation of orbit number and time since ANX used in the EO CFI (see EO_OPS for details).

### 7.1.7 Mean Local Solar Time Drift

The Mean Local Solar Time drift is the difference in angular velocity between the rate of change of the mean right ascension node and the motion of the mean Sun. This constant drift produces an increasing gap between the MLST of the ascending node and the angle measured from the line of nodes and the vernal equinox direction (see section 6.1.2). A constant rate at which the ANX MLST drifts per day (e.g. non-SunSynchronous Cryosat, with inclination at 92 deg , has a drift of about $-180 \mathrm{~s} / \mathrm{day}$ ). For a Sun-Synchronous orbit, the value should be 0.0 .

The relationship between MLST of subsequent days is the following:

$$
\mathrm{MLST}_{\mathrm{dayN}}=\mathrm{MLST}_{\mathrm{day}(\mathrm{~N}-1)}+\mathrm{MLST}_{\mathrm{drift}}
$$

Formula used to model the ANX MLST evolution:

$$
\begin{aligned}
& \text { ANX_MLST }=\text { ANX_MLST } \\
& \text { ref } \\
& +S H_{1} * \sin \left(\frac{2 \pi}{T_{1}} *\left(t-t_{\text {ref }}^{\text {harm1 }}\right)\right)+C H_{1} * \cos \left(\frac{2 \pi}{T_{1}} *\left(t-t_{r e f}^{\text {harm1 }}\right)\right) \\
& +S H_{2} * \sin \left(\frac{4 \pi}{T_{2}} *\left(t-t_{r e f}^{\text {harm2 }}\right)\right)+C H_{2} * \cos \left(\frac{4 \pi}{T_{2}} *\left(t-t_{r e f}^{\text {harm2 }}\right)\right)
\end{aligned}
$$

where:
L is the linear term,
Q is the quadratic term,
$\mathrm{SH}_{\mathrm{N}}$ and $\mathrm{CH}_{\mathrm{N}}$ are the amplitudes of the sine and cosine harmonics ( $1^{\text {st }}$ and $2^{\text {nd }}$ order), $\mathrm{t}_{\text {ref }}$ is the reference date ( $25^{\text {th }}$ October $201000: 00: 00 \mathrm{~h}$ ),
$\mathrm{t}_{\text {ref }}{ }^{\text {harmN }}$ are the reference date for the harmonics ( $\left(^{\text {st }}\right.$ and $2^{\text {nd }}$ order),
$\mathrm{T}_{\mathrm{N}}$ are the periods of the harmonics ( $1^{\text {st }}$ and $2^{\text {nd }}$ order).

### 7.1.8 Repeat Cycle and Cycle Length

In the geo/helio-synchronous orbits, the ground track repeats precisely after a constant integer number of orbits and a constant duration. The duration in days of that period is called the repeat cycle, whereas the corresponding number of orbits is called the cycle length.
The repeat cycle of a Sun-synchronous orbit is an integer number of days, while it is not an integer number when considering a non Sun-synchronous orbit. Thus, the orbit information contained within a scenario file comprises an integer repeat cycle plus a drift on it, to cope with non Sun-synchronous orbits. The true repeat cycle shall result from the following:

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$$
\text { TrueRepeatCycle }=\text { RepeatCycle }(1+\text { MLSTdrift })
$$

### 7.1.9 Sub-satellite Point, Satellite Nadir and Ground Track

The subsatellite point (SSP) is the normal projection of the position of the satellite in the orbit on to the surface of the Earth's Reference Ellipsoid. It is also referred as nadir.
The trace made by the subsatellite point on the surface of the Earth's Reference Ellipsoid due to the motion of the satellite along its orbit is called the ground track.

### 7.1.10 Mean Local Solar Time and True Local Solar Time

### 7.1.10.1 Mean Local Solar Time

The Mean Local Solar Time (MLST) is the difference between the right ascension of the selected point in the orbit RA and the mean longitude of the Sun L, expressed in hours.

$$
M L S T=(R A-L+\pi) \frac{24}{2 \pi}[\text { hours }]
$$

The mean longitude $\bar{L}$ of the Sun represents the motion of the mean Sun and is given, in the Mean of Date reference frame, by (FLANDERN reference):

$$
\bar{L}=280.46592+0.9856473516(\mathrm{t}-0.5)[\mathrm{deg}]
$$

where $t$ is the UT1 time expressed in the MJD2000 format.
The motion of the mean Sun has a constant mean longitude rate, namely $\dot{\bar{L}}=0.9856473516[\mathrm{deg} / \mathrm{s}]$.

### 7.1.10.2 True Local Solar Time

The True Local Solar Time (TLST) is the difference between the right ascension of the selected point in the orbit RA and the right ascension of the Sun RAsun, expressed in hours.

$$
T L S T=\left(R A-R A_{\text {Sun }}+\pi\right) \frac{24}{2 \pi}[\text { hours }]
$$

The RA $A_{\text {sun }}$ is calculated, in the Mean of Date reference frame, according to FLANDERN reference.
Mean and True Local Solar Time are normally expressed in hours considering the equivalence existing between hours and degrees; i.e. the Earth completes a complete revolution with respect to the Sun (360 degrees) in one day (24 hours).

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### 7.1.11 Phase and Cycle

The phase is considered to be a portion of the mission characterised by a ground track pattern different from the previous and following. Each time a change of repeat cycle period is applied, a new phase starts. The decision of starting a new phase is performed by the mission management.

A cycle is defined as a full completion of the repeat period. A cycle starts by definition on an ascending node crossing closest to the Greenwich Meridian.

### 7.1.12 Absolute and Relative Orbit Number

The absolute orbit number considers the orbits elapsed since the first ascending node crossing after launch.
The relative orbit number is a count of orbits from 1 to the number of orbits contained in a repeat cycle. The relative orbit number 1 corresponds to the orbit whose ascending node crossing is closest to the Greenwich Meridian (eastwards). The relative orbit number is incremented in parallel to the absolute orbit number up to the cycle length, when it is reset and the cycle number is incremented by one.

When an orbit change is introduced, the relative orbit number of the new orbit is calculated such that the definition of the relative orbit number 1 is kept in the new repeat cycle.

### 7.1.13 Track Number

The track number is a count of orbits from 1 to the number of orbits contained in a repeat cycle. The track number 1 corresponds to the orbit whose ascending node crossing is closest to the Greenwich Meridian (eastwards). Two subsequent track numbers are those which have the nearest longitude of its ascending node crossing. Track number counter is incremented eastwards.

Track number 1 and relative orbit number 1 correspond to the same orbit. Furthermore, it exists a one-toone relationship between track and relative orbit numbers within a repeat cycle.

### 7.1.14 Spacecraft Midnight

The Spacecraft Midnight (SMX) is the time just halfway the nadir day $\rightarrow$ night transition and the nadir night $\rightarrow$ day transition. Such transitions are times at which the Sun Zenith Angle (SZA, angle satellite-nadir-sun) is 90 deg. In the day $\rightarrow$ night transition, the SZA is increasing (i.e. there is a transition from SZA $<90$ to SZA $>90$ ). In the night $\rightarrow$ day transition the SZA is decreasing (i.e. there is a transition from SZA>90 to SZA<90).

### 7.2 Attitude Coordinate Systems Parameters

### 7.2.1 Attitude determination parameters

There are different ways for providing the attitude parameters in order to establish the transformations between the satellite reference frames:

## 1. Attitude Mispointing Angles:

The transformation from one satellite reference frame to another is accomplished by three consecutive rotations over the angles roll $\xi$, pitch $\eta$ and yaw $\zeta$ according to the Euler convention defined in section 7.7.

The time derivative of those angles are the roll, pitch and yaw rates.

Both those angles and their rates are a function of the selected attitude control mode (see attitude control section particular to each satellite).
Usually, these angles are used for transforming from the satellite orbital frame to the satellite nominal attitude frame. Frequently there are superimposed on them a set of mispointing angles that make the Satellite Nominal Attitude Reference frame transform to the Satellite Attitude Reference frame.

A rotation matrix capable of transforming a vector from Frame A into Frame B can be expressed in term of the pitch, roll and yaw as follows:

$$
\begin{aligned}
R_{A \rightarrow B} & =R_{z}(\text { yaw }) \cdot R_{x}(- \text { pitch }) \cdot R_{y}(- \text { roll }) \\
& =R_{z}(\zeta) \cdot R_{x}(-\eta) \cdot R_{y}(-\xi) \\
& =\left[\begin{array}{ccc}
\cos (\zeta) \cdot \cos (\xi)+\sin (\xi) \cdot \sin (\zeta) \cdot \sin (\eta) & \sin (\zeta) \cdot \cos (\eta) & \cos (\zeta) \cdot \sin (\xi)-\cos (r) \cdot \sin (\zeta) \cdot \sin (\eta) \\
-\sin (\zeta) \cdot \cos (\xi)+\sin (\xi) \cdot \sin (\eta) \cdot \cos (\zeta) & \cos (\zeta) \cdot \cos (\eta) & -\sin (\zeta) \cdot \sin (\xi)-\sin (\eta) \cdot \cos (\zeta) \cdot \cos (\xi) \\
-\sin (\xi) \cdot \cos (\eta) & \sin (\eta) & \cos (\xi) \cdot \cos (\eta)
\end{array}\right]
\end{aligned}
$$

where $v_{B}=R_{A \rightarrow B} v_{A}$ transforms a vector $v_{A}$ (defined in Frame A) into a vector $v_{B}$ (defined in Frame B).

The mispointing angles are expressed as three components, namely pitch $\Delta \eta$, roll $\Delta \xi$, and yaw $\Delta \zeta$. The time derivative of those mispointing angles are the mispointing rates.

## 2. Attitude Quaternions:

The previous transformations could be given via quaternions (also called Euler symmetric parameters) instead of angles.
Quaternions are base on Euler's theorem that given two coordinate systems, there is one invariant axis (e) along which measurements are the same in both coordinate systems and that is possible to move from one system to the other through a rotation $(\boldsymbol{\beta})$ about the axis $\boldsymbol{e}$. According to this theorem, the quaternions is defined as:

A rotation matrix (direction cosine matrix) is expressed in term of the quaternion parameters as follows:

$$
R=\left[\begin{array}{ccc}
q_{1}^{2}-q_{2}^{2}-q_{3}^{2}+q_{4}^{2} & 2\left(q_{1} q_{2}+q_{3} q_{4}\right) & 2\left(q_{1} q_{3}-q_{2} q_{4}\right) \\
2\left(q_{1} q_{2}-q_{3} q_{4}\right) & -q_{1}^{2}+q_{2}^{2}-q_{3}^{2}+q_{4}^{2} & 2\left(q_{2} q_{3}+q_{1} q_{4}\right) \\
2\left(q_{1} q_{3}+q_{2} q_{4}\right) & 2\left(q_{2} q_{3}-q_{1} q_{4}\right) & -q_{1}^{2}-q_{2}^{2}+q_{3}^{2}+q_{4}^{2}
\end{array}\right]=\left[\begin{array}{ccc}
X_{x} & Y_{x} & Z_{x} \\
X_{y} & Y_{y} & Z_{y} \\
X_{z} & Y_{z} & Z_{z}
\end{array}\right]
$$

Notice that the conversion of a quaternion to a rotation matrix results in the basis vectors $\mathrm{X}, \mathrm{Y}, \mathrm{Z}$, which become columns vectors of the rotation matrix - n.b. the conversions in the EOCFI API take as input or calculate the basis vectors as separate vectors. Also, X, Y and Z are the unitary direction vectors along the $\mathrm{X}, \mathrm{Y}$, and Z -axis, respectively, of the source frame (expressed in the target frame).

When calculating the quaternion equivalent to a rotation matrix R , the EOCFI follows the algorithm proposed by [SHOEMAKE]:

$$
\text { when } X_{x}+Y_{y}+Z_{z}>0 \text {, the solution is } \mathbf{q}=\left[\begin{array}{c}
\frac{1}{2 s}\left(Y_{z}-Z_{y}\right) \\
\frac{1}{2 s}\left(Z_{x}-X_{z}\right) \\
\frac{1}{2 s}\left(X_{y}-Y_{x}\right) \\
\frac{s}{2}
\end{array}\right] \text {, with } s=\sqrt{X_{x}+Y_{y}+Z_{z}+1}
$$

otherwise, when $X_{x}>Y_{y}$ and $X_{x}>Z_{z}$, the solution is $\mathbf{q}=\left[\begin{array}{c}\frac{s}{2} \\ \frac{1}{2 s}\left(X_{y}+Y_{x}\right) \\ \frac{1}{2 s}\left(Z_{x}+X_{z}\right) \\ \frac{1}{2 s}\left(Y_{z}-Z_{y}\right)\end{array}\right]$, with $s=\sqrt{X_{x}-Y_{y}-Z_{z}+1}$
$\begin{aligned} \text { otherwise, when } Y_{y}>Z_{z} \text {, the solution is } \mathbf{q} & =\left[\begin{array}{c}\frac{1}{2 s}\left(X_{y}+Y_{x}\right) \\ \frac{s}{2} \\ \frac{1}{2 s}\left(Y_{z}+Z_{y}\right) \\ \frac{1}{2 s}\left(Z_{x}-X_{z}\right)\end{array}\right] \text {, with } s=\sqrt{-X_{x}+Y_{y}-Z_{z}+1} \\ \text { otherwise, the solution is } \mathbf{q} & =\left[\begin{array}{c}\frac{1}{2 s}\left(Z_{x}+X_{z}\right) \\ \frac{1}{2 s}\left(Y_{z}+Z_{y}\right) \\ \frac{s}{2} \\ \frac{1}{2 s}\left(X_{y}-Y_{x}\right)\end{array}\right] \text {, with } s=\sqrt{-X_{x}-Y_{y}+Z_{z}+1}\end{aligned}$

## 3. AOCS Rotation Amplitudes

The AOCS rotation amplitudes are the three constants $\mathrm{Cx}, \mathrm{Cy}$ and Cz that define the transformation from the Satellite Nominal Attitude to the Satellite Attitude Reference frame according to the selected attitude control mode (see attitude control section particular to each satellite).

### 7.2.2 Satellite Centered Direction

The parameters that define a direction in a Satellite Reference frame are the satellite related azimuth and the satellite related elevation. If $x, y, z$ are the axis in the Satellite Reference frame, the azimuth and elevation are defined in the following way (check Figure 12Figure 12):

- Azimuth: the angle in the xy plane from -y axis to the projection of the pointing direction in the xy plane; the angle direction is taken from -y axis to -x axis.
- Elevation: the angle from the projection of the pointing direction in the xy plane to the pointing direction itself, measured from xy plane to - z axis.


Figure 12: Azimuth and elevation definition

Considering a given elevation (el) and azimuth (az), the unitary LoS direction vector (u) can be specified as:

$$
\begin{aligned}
& u_{x}=-\sin (a z) \cos (e l) \\
& u_{y}=-\cos (a z) \cos (e l) \\
& u_{z}=-\sin (e l)
\end{aligned}
$$

From a unitary LoS direction vector (u), the elevation (el) and azimuth (az) can be determined as:

$$
\begin{aligned}
a z & =\arctan 2\left(-u_{x},-u_{y}\right) \\
e l & =-\arcsin \left(u_{z}\right)
\end{aligned}
$$

### 7.3 Earth-related Parameters

Note that altitude refers always to geodetic altitude except when the contrary is explicitly said.

### 7.3.1 Geodetic Position

The geodetic coordinates of a point, related to the Earth's Reference Ellipsoid, are the geocentric longitude $\lambda$, geodetic latitude $\varphi$, and geodetic altitude h , represented in



Figure 13.
The geocentric latitude $\varphi$ ', geocentric radius $\rho$ and the geocentric distance $d$ are also represented in



Figure 13.
The parameters $\mathbf{a}, \mathbf{e}$ and $\mathbf{f}$, i.e. the semi-major axis, the first eccentricity and the flattening of the Earth's Reference Ellipsoid (see section 8.2.2), define the equations that express these other parameters.


Figure 13: Geodetic position

The geocentric latitude $\varphi$ ' and the geodetic latitude $\varphi$ are related by the expression, only valid on ellipsoid:

$$
\tan (\varphi)=\frac{1}{(1-f)^{2}} \tan \left(\varphi^{\prime}\right)
$$

The geocentric radius $\rho$ is calculated with:

$$
\rho=\frac{a \sqrt{1-e^{2}}}{\sqrt{1-e^{2} \cos ^{2} \varphi^{\prime}}}
$$

The relationship between the cartesian coordinates of a point and its geodetic coordinates is:

$$
\begin{aligned}
& x=(N+h) \cos (\varphi) \cos (\lambda) \\
& y=(N+h) \cos (\varphi) \sin (\lambda) \\
& z=\left[\left(1-e^{2}\right) N+h\right] \sin (\varphi)
\end{aligned}
$$

where N is the East-West radius of curvature:

$$
N=\frac{a}{\sqrt{1-e^{2} \sin ^{2} \varphi}}
$$

The inverse transformation, from the cartesian to the geodetic coordinates, cannot be performed analytically. The iterative method that will be used will be initialized according to (BOWRING reference).
The normal projection of a point on the surface of the Earth's Reference Ellipsoid is called Nadir, and when that point corresponds to the position of the satellite, the projection is called subsatellite point.

Another important radius of curvature is M, the North-South radius of curvature:

$$
M=\frac{a\left(1-e^{2}\right)}{\sqrt{\left(1-e^{2} \sin ^{2} \varphi\right)^{3}}}
$$

Code:

The radius of curvature in any selected direction $\mathrm{R}_{\mathrm{Az}}$ can be calculated with the expression:

$$
\frac{1}{R_{A z}}=\frac{\cos ^{2}(A z)}{M}+\frac{\sin ^{2}(A z)}{N}
$$

where Az is the angle of the selected direction expressed in the Topocentric reference frame.
The satellite centred aspect angle $\alpha_{s / c}$ is the angle measured at the satellite between the geometric direction ${ }^{5}$ from the satellite to the subsatellite point and the geometric direction from the satellite to the centre of the Earth.

The geocentric aspect angle $\alpha_{\mathrm{g}}$ is the angle measured at the centre of the Earth between the geometric direction from the Earth centre to the subsatellite point and the geometric direction from the Earth centre to the satellite.
The subsatellite point centred aspect angle $\alpha_{\text {ssp }}$ is the angle measured at the subsatellite point between the geometric direction from the subsatellite point to the satellite and the geometric direction from the subsatellite point to the centre of the Earth.
The geodesic distance or ground range between two points that lay on an ellipsoid is by definition the minimum distance between those two points measured over that ellipsoid.
The velocity $\overrightarrow{v_{E}}$ and $\overrightarrow{a_{E}}$ acceleration relative to the Earth, i.e the Earth's Reference Ellipsoid, of a point that lays on its surface can be split into different components.

- Northward component $=\vec{v}_{E} \cdot \vec{N}$ or $\vec{a}_{E} \cdot \vec{N}$
- Eastward component $=\vec{v}_{E} \cdot \vec{E}$ or $\vec{a}_{E} \cdot \vec{E}$
- Ground track tangential component $=\overrightarrow{v_{E}} \cdot \dot{t}=v_{E}$ or $\overrightarrow{a_{E}} \cdot \dot{t}$
- Magnitude $=v_{E}=\left|\vec{v}_{E}\right|$ or $\quad a_{E}=\left|\vec{a}_{E}\right|$
- Azimuth $=$ the azimuth of the $\overrightarrow{v_{E}}$ and $\overrightarrow{a_{E}}$ vectors measured in the Topocentric reference frame
where $\vec{N}$ and $\vec{E}$ are the north and east direction axes of the Topocentric reference frame centred on that point, and $t$ is the unitary vector tangent to the ground track at that point.

[^2]Code:
EO-MA-DMS-GS-

### 7.3.2 Earth Centered Direction

The parameters that define a direction from the centre of the Earth to a point in the Mean of Date reference frame are the right ascension $(\alpha)$ and the declination $(\delta)$, shown in next figure:
$+\mathrm{x}=$ Pointing towards mean vernal equino x
$+\mathrm{z}=$ Pointing towards north pole
$+\mathrm{y}=\mathrm{z} \wedge \mathrm{x}$
Right Ascension: from +x over +y
Declination: from $+\mathrm{x}+\mathrm{y}$ plane towards +z

$\sim$ Mean Vernal Equinox
Figure 14: Earth centred direction

### 7.3.3 Topocentric Direction

The parameters that define a direction in the Topocentric reference frame are the topocentric azimuth (Az) and the topocentric elevation (El), represented in the next drawing:


Figure 15: Topocentric direction

### 7.4 Ground Station Parameters

### 7.4.1 Ground Station Location

The location of a Ground Station is defined by its geodetic parameters: i.e. geocentric longitude $\lambda$, geodetic latitude $\varphi$, and geodetic altitude h with respect to the Earth's Reference Ellipsoid.

Code:
EO-MA-DMS-GS-

### 7.4.2 Ground Station Visibility

The visibility of a point from a Ground Station is limited by the minimum link elevation at which that point must be in order for the link between that Ground Station and that point to be established.
That minimum topocentric elevation is expressed in the Topocentric reference frame centred at that Ground Station (see section 7.3.3), and although it is ideally a constant, in fact a real Ground Station usually has a physical mask that makes the minimum topocentric elevation be a function of the topocentric azimuth.

### 7.5 Target Parameters

### 7.5.1 Moving and Earth-fixed Targets

A target $\vec{r}_{t}$ is a point that is observed from the satellite and that satisfies certain conditions.
The look direction, or line of sight (LOS), $\vec{u}_{0}$ is the light direction, at the satellite, of the path followed by the light in its travel from the target to the satellite.
If the target moves with respect to the Earth, as a result of a change in the satellite position or a change in the look direction, it is called the moving target.
If the target is fixed with respect to the Earth, which implies that if the satellite position changes then the look direction has to change in the precise way to keep looking to that particular point fixed to the Earth, it is called the Earth fixed target.
In other words, the velocity of the moving target is the result of the motion of the satellite and the change in the look direction, or in the conditions that define it, with time. On the other hand, the velocity of the Earth fixed target is only a function of the position of that point with respect to the Earth's Reference Ellipsoid and the rotation of the Earth fixed reference frame.

### 7.5.2 Location Parameters

The location of a target is defined by its geodetic parameters: i.e. geocentric longitude $\lambda$, geodetic latitude $\varphi$, and geodetic altitude $h$ with respect to the Earth's Reference Ellipsoid, although it also can be defined by its cartesian position vector ( $\mathrm{x}, \mathrm{y}, \mathrm{z}$ ) expressed in the Earth fixed reference frame.

### 7.6 Sun and Moon Parameters

The Sun semi-diameter $\mathrm{D}_{\text {Sun }}$ is the apparent semi-diameter of the Sun, expressed in radians, as seen from the satellite, and is calculated with the equation:

$$
D_{\text {sun }}=\frac{d_{\text {Sun }}}{R_{\text {sun }-s c}}
$$

where $\mathrm{d}_{\text {Sun }}=6.96 \times 10^{8}[\mathrm{~m}]$ is the semi-diameter of the Sun, and $\mathrm{R}_{\text {Sun-S/C }}$ is the geometric distance between the satellite and the Sun centre.

The Moon semi-diameter $\mathrm{D}_{\text {Moon }}$ is the apparent semi-diameter of the Moon, expressed in degrees, as seen from the satellite, and is calculated with the equation:

$$
D_{\text {Moon }}=\frac{d_{\text {Moon }}}{R_{\text {Moon-SC }}}
$$

where $d_{\text {Moon }}=1738000[\mathrm{~m}]$ is the semi-diameter of the Moon, and $\mathrm{R}_{\text {Moon-S/C }}$ is the geometric distance between the satellite and the Moon centre.
The area of the Moon lit by the Sun $\mathrm{A}_{\text {Moon-Sun }}$ is calculated with the expression:

$$
A_{\text {Moon-Sun }}=\frac{1+\cos \theta_{\text {Sun }- \text { Moon }-S C}}{2}
$$

where $\theta_{\text {Sun-Moon-S/C }}$ is the angle measured at the centre of the Moon between the geometric direction from the centre of the Moon to the centre of the Sun and the geometric direction from the centre of the Moon to the satellite.

If $\mathrm{A}_{\text {Moon-Sun }}=0$ it is a new Moon, and if $\mathrm{A}_{\text {Moon-Sun }}=1$ it is a full Moon
The satellite eclipse flag indicates whether or not the path followed by the light from the centre of the Sun to the satellite intersects the Earth's Reference Ellipsoid. It is equivalent to the satellite to Sun visibility flag.

The satellite to Moon visibility flag indicates whether or not the path followed by the light from the centre of the Moon to the satellite intersects the Earth's Reference Ellipsoid.

The target to Sun visibility flag indicates whether or not the path followed by the light from the centre of the Sun to the target intersects the Earth's Reference Ellipsoid.

### 7.7 Euler angles

The Earth Observation CFI applies the following convention when using Euler angles to rotate one reference frame to another.

The rotated reference frame ( X 's, $\mathrm{Y}^{\prime}$ 's, Z's) is obtained by applying three consecutive rotations to the original reference frame:

1. Rotation around -Ys over a roll angle $\xi$
2. Rotation around $-X^{1}$ s (i.e the rotated Xs) over a pitch angle $\eta$
3. Rotation around $+Z^{2}$ s (i.e the rotated $Z^{1} s$ ) over a yaw angle $\zeta$.

The next figure depicts the three rotations, using 90 degrees rotations as example - the figure presents the rotation axis in blue, the axes before rotation in red and axes after rotation in green.

Code:
Date:
Issue:


Figure 16: Euler Angles

## 8 MODELS

### 8.1 Attitude Modes

The Satellite Nominal reference frame (SNRF), presented in section 5.2.2, can be configured with the following three axes stabilized Attitude Modes:

- Generic Pointing Mode (GPM)
- Yaw Steering Mode (YSM)
- Local Normal Pointing (LNP)
- Zero-Doppler Pointing (ZDOP)
- Geocentric Pointing (GP)


### 8.1.1 Generic Pointing Mode

The Generic Pointing Mode (GPM) allows the user to define the Satellite Nominal Reference Frame (SNRF) in the most generic way by defining the following properties:

- The PRIMARY axis and direction (+/-X, +/-Y, +/- Z);
- The PRIMARY axis target (see list below);
- The SECONDARY axis and direction (+/-X, +/-Y, +/- Z, different from primary axis);
- The SECONDARY axis target (see list below).

Based on the properties above, the SNRF is defined as follows:

- The primary axis (with direction) is aligned to the primary axis target;
- The secondary axis (with direction) is aligned to the vector obtained by computing the cross-product between primary axis (positive direction) and the secondary target axis;
- The tertiary axis completes the right-hand frame together with primary and secondary axes.

There are many possible choices in the definition of the axis target, for example:

- Sun pointing
- Moon pointing
- Earth pointing
- Nadir pointing
- Inertial velocity pointing
- Earth Fixed velocity pointing
- Inertial target pointing
- Earth Fixed target pointing
- Earth Fixed Satellite position

Code:

Given the usefulness of some specific configurations of the Generic Pointing Mode, a set of custom pointing modes is supported (more details in section 8.1.2). As expected, these custom pointing modes are just specific instances of the Generic Pointing Mode; for example, the Yaw Steering Mode shown in Table 4 defines the SNRF axes as follows:

- the negative Z axis is aligned with the satellite position vector in the Earth Fixed reference system;
- the positive X axis is aligned with the cross product of Z axis and the velocity in the Earth Fixed reference system;
- the Y axis is computed according to right-hand rule.


### 8.1.2 Custom Pointing Modes

Yaw Steering Mode (YSM), Local Normal Pointing (LNP), Zero-Doppler Pointing (ZDP), and Geocentric Pointing (GP) modes are special cases of Generic Pointing Modes, with axes and targets that are predefined according to the following table:
Table 4: Attitude control modes

| Attitude <br> Mode | Primary <br> Axis | Primary Axis <br> Target | Secondary <br> Axis | Secondary Axis <br> Target |
| :--- | :--- | :--- | :--- | :--- |
| YSM | -Z | Nadir | + +X | EF Velocity |
| LNP | -Z | Nadir | + X | Inertial Velocity |
| ZDOP | -Y | EF Velocity | -X | Nadir |
| GP | Z | EF Satellite <br> Position | + X | Inertial Velocity |

### 8.2 Earth

### 8.2.1 Earth Position

The position and velocity of the Earth in the Barycentric and Heliocentric Mean of 2000 reference frames will be calculated according to FLANDERN reference.

### 8.2.2 Earth Geometry

The geometry of the Earth is modeled by a Reference Ellipsoid. Different definitions of reference ellipsoids can be found hereafter in Table 5 .

Table 5: WGS84 parameters

| Parameter | Notation | WGS 84 |
| :--- | :---: | :--- |
| Semi major axis $(\mathrm{m})$ | a | 6378137 |
| Flattening $=(\mathrm{a}-\mathrm{b}) / \mathrm{a}$ | f | $1 / 298.257223563$ |
| First Eccentricity $=\left(\mathrm{a}^{2}-\mathrm{b}^{2}\right) / \mathrm{a}^{2}$ | e | 0.0818191908426 |
| Semi minor axis $(\mathrm{m})$ | b | 6356752.3142 |

Code:

The minimum distance between two points located on an ellipsoid is the length of the geodesic that crosses those two points. This geodesic distance will be calculated according to HEISKANEN reference.
The surface at a certain geodetic altitude $\boldsymbol{h}$ over the Earth's Reference Ellipsoid is defined by:

$$
\begin{aligned}
& x=(N+h) \cos (\varphi) \cos (\lambda) \\
& y=(N+h) \cos (\varphi) \sin (\lambda) \\
& z=\left[\left(1-e^{2}\right) N+h\right] \sin (\varphi)
\end{aligned}
$$

where N is the radius of curvature parallel to the meridian:

$$
N=\frac{a}{\sqrt{1-e^{2} \sin ^{2} \varphi}}
$$

and $\varphi$ and $\lambda$ are the geodetic latitude and geocentric longitude of a point on that ellipsoid.
Nevertheless, the surface at a certain geodetic altitude h over the Earth's Reference Ellipsoid will be modelled as another ellipsoid, concentric with it, and with (a+h) and (b+h) as semi-major and semi-minor axis.

This simplification is quite accurate and have the advantage that allows the analytical calculation of the intersection or tangent points with such a surface.

### 8.2.3 Earth Atmosphere

The Earth atmosphere can be represented by different models. The selection of a certain atmosphere model depends upon the requirements imposed by the mission definition. It could include certain simplifications to the generic definition.

It is also assumed that the atmosphere rotates with the same angular velocity as the Earth.
The definition of the Earth atmosphere is important for instrument pointing task and refraction.

### 8.2.3.1 US Standard Atmosphere 1976

The U.S Standard Atmosphere 1976 Atmosphere model is modified as follows:

- it ranges from $Z=0 \mathrm{Km}$ to $\mathrm{Z}=86 \mathrm{Km}$.
- the ratio $\mathrm{M} / \mathrm{M}_{0}$ decreases linearly from $\mathrm{Z}=80$ to $\mathrm{Z}=86 \mathrm{Km}$.
- the linear relationship between $\mathrm{T}_{\mathrm{M}}$ and H is replaced by either an arc of a circle or by a polynomial function in the vicinity of the points where the molecular-scale temperature gradient changes, in order to have a continuous and differentiable function $T_{M}=f(H)$
The U.S Standard Atmosphere 1976 is defined as follows (STD76 reference):
- The air is assumed to be dry, and at altitudes sufficiently below 86 Km , the atmosphere is assumed to be homogeneously mixed with a relative-volume composition leading to a constant mean molecular weight M .
- The air is treated as if it were a perfect gas, and the total pressure $P$, temperature $T$, and total density $\rho$ at any point in the atmosphere are related by the equation of state, i.e. the perfect gas law, one form of which is:

$$
P=\frac{\rho R T}{M}
$$

where $\mathrm{R}=8.31432 \times 10^{3}[\mathrm{Nm} /(\mathrm{KmolK})]$ is the universal gas constant.

- Besides the atmosphere is assumed to be in hydrostatic equilibrium, and to be horizontally stratified so that dP , the differential of pressure, is related to dZ , the differential of geometric altitude, by the relationship:

$$
d P=-g \rho d Z
$$

where g is the altitude-dependent acceleration of gravity, which can be calculated with the expression:

$$
g=g_{0}\left(\frac{r_{0}}{r_{0}+Z}\right)^{2}
$$

where $\mathrm{r}_{0}=6356766[\mathrm{~m}]$ and $\mathrm{g}_{0}=9.80665\left[\mathrm{~m} / \mathrm{s}^{2}\right]$, and that yields:

$$
H=\frac{r_{0} Z}{r_{0}+Z}
$$

where H is the geopotential altitude.

- The molecular-scale temperature $\mathrm{T}_{\mathrm{M}}$ at a point is defined as:

$$
T_{M}=T \frac{M_{0}}{M}
$$

where $\mathrm{M}_{0}=28.9644[\mathrm{Kg} / \mathrm{Kmol}]$ is the sea-level value of M .
In the region from $Z=0 \mathrm{Km}$ to $Z=80 \mathrm{Km} \mathrm{M}$ is constant and $M=M_{0}$, whereas between $Z=80 \mathrm{Km}$ and $\mathrm{Z}=86 \mathrm{Km}$, the ratio $\mathrm{M} / \mathrm{M}_{0}$ is assumed to decrease from 1.000000 to 0.999578
Up to altitudes up to 86 Km the function $\mathrm{T}_{\mathrm{M}}$ versus H is expressed as a series of seven successive linear equations. The general form of these linear equations is:

$$
T_{M}=T_{M, b}+L_{M, b}\left(H-H_{0}\right)
$$

The value of $\mathrm{T}_{\mathrm{M}, \mathrm{b}}$ for the first layer $(\mathrm{b}=0)$ is $288.15[\mathrm{~K}]$, identical to $\mathrm{T}_{0}$ the sea-level value of T . The six values of $\mathrm{H}_{\mathrm{b}}$ and $\mathrm{L}_{\mathrm{M}, \mathrm{b}}$ are:

Table 6: Molecular-scale temperature coefficients

| Subscript | Geopotential altitude $\mathbf{H}_{\mathrm{b}}[\mathbf{K m}]$ | Molecular-scale temperature <br> gradient $\mathbf{L M}, \mathbf{b}[\mathbf{K} / \mathbf{K m}]$ |
| :---: | :---: | :---: |
| 0 | 0 | -6.5 |
| 1 | 11 | 0.0 |
| 2 | 20 | 1.0 |
| 3 | 32 | 2.8 |
| 4 | 47 | 0.0 |
| 5 | 51 | -2.8 |
| 6 | 71 | -2.0 |
| 7 | $84.8520(\mathrm{Z}=86)$ |  |

Finally, the pressure can be calculated with the following expressions:

$$
\begin{array}{ll}
P=P_{b}\left(\frac{T_{M, b}}{T_{M, b}+L_{M, b}\left(H-H_{b}\right)}\right)^{\frac{g_{0} M_{0}}{R L_{M, b}}}\left(\mathrm{~L}_{M, \mathrm{~b}} \neq 0\right) \\
P=P_{b} \exp \left[\frac{-g_{0} M_{0}\left(H-H_{b}\right)}{R T_{M, b}}\right] & \left(\mathrm{L}_{M, b}=0\right)
\end{array}
$$

The reference-level value for $\mathrm{P}_{\mathrm{b}}$ for $\mathrm{b}=0$ is the defined sea-level value $\mathrm{P}_{0}=101325.0 \mathrm{~N} / \mathrm{m}^{2}$. Values of $\mathrm{P}_{\mathrm{b}}$ for $\mathrm{b}=1$ through $\mathrm{b} \geq 6$ are obtained from the application of the appropriate equation above for the case when $\mathrm{H}=\mathrm{H}_{\mathrm{b}+1}$.

### 8.2.4 Refractive index

The refractive index is calculated with the Edlen's law (EDLEN) although neglecting the contribution of the partial pressure of the water vapor.

### 8.2.4.1 Edlen's law

The relative refraction index $m$ at any point in the atmosphere is calculated by:

$$
\begin{aligned}
& m=1+N \times 10^{-6} \\
& \text { with } N=\left[a_{0}+\frac{a_{1}}{1-\left(\frac{v}{b_{1}}\right)^{2}}+\frac{a_{2}}{1-\left(\frac{v}{b_{2}}\right)^{2}}\right] \frac{P}{P_{0}} \frac{\left(T_{0}+15,0\right)}{T}-\left[c_{0}-\left(\frac{v}{c_{1}}\right)^{2}\right] \frac{P_{w}}{P_{0}}
\end{aligned}
$$

where P is the total air pressure in $\mathrm{mb}, \mathrm{T}$ is the temperature in $\mathrm{K}, \mathrm{P}_{0}=1013.25 \mathrm{mb}, \mathrm{T}_{0}=273.15 \mathrm{~K}, \mathrm{P}_{\mathrm{w}}$ is the partial pressure of water vapour in mb , and $v=10^{4} / \lambda$ is the frequency in $\mathrm{cm}^{-1}$ for the wavelength $\lambda$ in micrometers (EDLEN)

The constants in that equation are:
$\mathrm{a}_{0}=83.42$
$a_{1}=185.08$
$\mathrm{a}_{2}=4.11$
$\mathrm{b}_{1}=1.140 \times 10^{5}$
$\mathrm{b}_{2}=6.24 \times 10^{4}$
$\mathrm{c}_{0}=43.49$
$\mathrm{c}_{1}=1.70 \times 10^{4}$

The total air pressure and the temperature will be the corresponding to the atmosphere previously described, and the term in the last equation that corresponds to the partial pressure of water vapor will be neglected and therefore not calculated.

### 8.2.5 Digital Elevation Models (DEM)

The digital elevation model of the Earth consists in a set of points defining a grid for which a measure of the altitude over the Earth reference ellipsoid is given.
In the following table the supported DEMs are listed:

| DEM name | Resolution | URL |
| :--- | :---: | :--- |
| GETASSE30 (versions 1,2,3) | $30 \operatorname{arcsec}$ | http://earth.esa.int/services/amorgos/download/getasse/ |
| ACE2 | 3 arcsec <br> 9 arcsec <br> 30 arcsec <br> 5 min | http://tethys.eaprs.cse.dmu.ac.uk/ACE2/shared/overview |
| ASTER GDEM (Versions 2, 3) | 1 arcsec | https://lpdaac.usgs.gov/products/astgtmv002/ |
| https://lpdaac.usgs.gov/products/astgtmv003/ |  |  |

GETASSE30 and ACE2 DEM can be downloaded also from this URL:
http://eop-cfi.esa.int/index.php/mission-cfi-software/eocfi-software/support-files (registration required)

### 8.3 Sun and Moon

Sun and Moon position and velocity in the True of Date reference frame will be calculated according to FLANDERN reference.

### 8.4 Stars

To calculate the look direction from the satellite to a star, two consecutive steps must be performed:

- To calculate the stars coordinates in the Mean of Date reference frame at the current epoch, taking as input a star catalogue (assumed to be expressed in the Barycentric Mean of 2000.0 reference frame for the epoch J2000.0).
- To calculate the star coordinates in the Satellite Relative Actual Reference frame at the same epoch.

The first step must apply the following corrections:

Table 7: First step correction of star looking direction

| Correction | Description | Effect |
| :--- | :--- | :--- |
| Proper motion | Intrinsic motion of the star across the <br> background with respect to a reference <br> epoch (e.g J2000.0) leading to a change <br> in the apparent star position at the current <br> epoch | Lower than 0.3 mdeg/year |
| Annual parallax | Apparent displacement of the position of <br> the star caused by the difference in the <br> position of the barycenter and the <br> position of the Earth with the motion of <br> the Earth around the Sun during the year | Lower than 0.3 mdeg |
| Light deflection | Gravitational lens effect of the Sun | Lower than 500 $\mu$ deg at the <br> limb of the Sun and falling off <br> rapidly with distance, e.g. to 6 <br> $\mu$ (eg at an elongation of 20 deg <br> (so it will be ignored) |
| Annual aberration | Apparent displacement of the position of <br> the star caused by the finite speed of light <br> combined with the motion of the Earth <br> around the Sun during the year | Lower than 6 mdeg <br> Precession |
| Change of the position of the star caused <br> by the transformation from the <br> Geocentric Mean of 2000.0 to the Mean <br> of Date reference frame | Lower than 6.0 mdeg/year |  |

whereas the second step must apply the following ones:
Table 8: Second step corrections of star looking direction

| Correction | Description | Effect |
| :---: | :---: | :---: |

Code:

| Satellite parallax | Apparent displacement of the position of <br> the star caused by the difference in the <br> position of the satellite and the position <br> of the Earth with the motion of the <br> satellite around the Earth during an orbit | Lower than $0.015 \mu \mathrm{deg}$ even for <br> ignored) |
| :--- | :--- | :--- |
| Satellite aberration | Apparent displacement of the position of <br> the star caused by the finite speed of light will be <br> combined with the motion of the satellite <br> around the Earth during an orbit | Lower than 1 mdeg for LEO <br> spacecraft |

### 8.4.1 Stars Positions

To apply some of the necessary corrections to calculate the coordinates of a star in the Satellite Relative Actual Reference frame, the following expressions shall be used (ALMAN95 reference):

- Get the following variables from a star catalogue:
- Right ascension at J2000.0 expressed in the Barycentric Mean of 2000.0: $\alpha_{0}[\mathrm{rad}]$
- Declination at J2000.0 expressed in the Barycentric Mean of 2000.0: $\delta_{0}[\mathrm{rad}]$
- Proper motion in the right ascension: $\mu_{\alpha}[\mathrm{rad} /$ century $]$
- Proper motion in the declination: $\mu_{\delta}$ [rad/century]
- Radial velocity: $v$ [au/century]
- Parallax: $\pi$ [rad]
- Correct the star position obtained from the star catalogue $\left(\alpha_{0}, \delta_{0}\right)$ for the proper motion and annual parallax effects using the expressions:

$$
\begin{aligned}
& \overline{\mathrm{q}}=\left(\cos \alpha_{0} \cos \delta_{0}, \sin \alpha_{0} \cos \delta_{0}, \sin \delta_{0}\right) \\
& \overline{\mathrm{m}}=\left(\mathrm{m}_{\mathrm{x}}, \mathrm{~m}_{\mathrm{y}}, \mathrm{~m}_{\mathrm{z}}\right) \\
& \mathrm{m}_{\mathrm{x}}=-\mu_{\alpha} \cos \delta_{0} \sin \alpha_{0}-\mu_{\delta} \sin \delta_{0} \cos \alpha_{0}+v \pi \cos \delta_{0} \cos \alpha_{0} \\
& \mathrm{~m}_{\mathrm{y}}=\mu_{\alpha} \cos \delta_{0} \cos \alpha_{0}-\mu_{\delta} \sin \delta_{0} \sin \alpha_{0}+v \pi \cos \delta_{0} \sin \alpha_{0} \\
& \mathrm{~m}_{\mathrm{z}}=\mu_{\delta} \cos \delta_{0}+v \pi \sin \delta_{0} \\
& \overline{\mathrm{P}}=\overline{\mathrm{q}}+\mathrm{T} \overline{\mathrm{~m}}-\pi \bar{r}_{\mathrm{B}, \text { Earth }}
\end{aligned}
$$

where $\mathrm{T}=(\mathrm{t}-0.5) / 36525$, and t is the current TDT expressed in the MJD2000 format, and $\vec{r}_{B, E a r t h}$ is the position of the Earth in AU at that TDT, expressed in the Barycentric Mean of 2000 reference frame.

Code:

- Correct the star position for the annual aberration effect, using the following expressions:
$\overline{\mathrm{p}}_{2}=\frac{\frac{\overline{\mathrm{p}}_{1}}{\beta}+\left(1+\frac{\overline{\mathrm{p}}_{1} \bullet \overline{\mathrm{v}}}{1+\frac{1}{\beta}}\right)}{1+\overline{\mathrm{p}}_{1} \bullet \overline{\mathrm{v}}}$
$\overline{\mathrm{v}}=\frac{\overline{\mathrm{v}}_{\mathrm{B}, \text { Earth }}}{\mathrm{c}}=0.0057755 \overline{\mathrm{v}}_{\mathrm{B}, \text { Earth }}$
$\beta=\frac{1}{\sqrt{1-|\overline{\mathrm{v}}|^{2}}}$
where $\vec{v}_{B, E a r t h}$ is the velocity of the Earth in AU/d at the current TDT expressed in the Barycentric Mean of 2000 reference frame.
- The satellite aberration can be calculated with the expression (IERS_SUPL reference):
$\Delta \theta=\operatorname{asin}\left(\frac{v}{c} \sin \theta-\frac{1}{4}\left(\frac{v}{c}\right)^{2} \sin 2 \theta\right)[\mathrm{rad}]$
where $\Delta \theta$ is the change in the look direction from the satellite to the star, v is the velocity of the satellite expressed in the True of Date reference frame, and c is the velocity of the light in a vacuum.
- The following drawing sketches the satellite aberration:


Figure 17: Satellite aberration

Code:

### 8.5 Ray tracing

The path followed by the light when it crosses the Earth's atmosphere is bent due to the effect of the atmospheric refraction, and therefore the direction of the light when it enters the atmosphere $\overrightarrow{u_{E}}$ is different to the direction of the light when it leaves the atmosphere $\overrightarrow{u_{L}}$.
This effect is depicted in the following drawing:


Figure 18: Ray path

Note that this drawing also represents the satellite position $\overrightarrow{r_{S C}}$, the tangent point of the light path over the Earth's Reference Ellipsoid $\overrightarrow{r_{T}}$ and the corresponding tangent altitude $\mathrm{h}_{\mathrm{T}}$, the maximum angular deviation of the light path at the entrance $\theta_{\mathrm{E}}$ and at the exit $\theta_{\mathrm{L}}$ of the atmosphere, where:

$$
\cos \theta_{E}=\cos \theta_{L}=\overrightarrow{u_{E}} \cdot \overrightarrow{u_{L}}
$$

The geometric distance $\mathrm{R}_{\mathrm{T}, \mathrm{g}}$ between the satellite position and the tangent point is defined as:

$$
R_{T, g}=\left|\overrightarrow{r_{T}}-\overrightarrow{r_{S C}}\right|
$$

Finally, the range $\mathrm{S}_{\mathrm{T}}$ is the actual distance between those two points measured along the path.
A ray tracing model calculates the path followed by the light from the satellite through the atmosphere to the observation target.

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Code:
EO-MA-DMS-GS-

### 8.5.1 No refraction model

This is the simplest model as the effect of the atmospheric refraction is not considered, therefore the path followed by the light is approximated by a straight line.

The advantage of this model is that is purely analytical.

### 8.5.2Refraction models

There are two refraction ray tracing models, both based on the three following assumptions:

- The relative refractive index is a function only of the geometric altitude H above the Earth's Reference Ellipsoid, i.e. the Earth's atmosphere model is based on the assumption that the longitude or latitude variations of the relative refraction index are negligible
- The surface at a certain geometric altitude H will be modeled as an ellipsoid, concentric with the Earth's Reference Ellipsoid, with $(\mathrm{a}+\mathrm{H})$ and $(\mathrm{b}+\mathrm{H})$ as semi-major and semi-minor axis.
- The light path lays in a plane: this plane is defined by the satellite position vector $\overrightarrow{r_{S C}}$, and by the known light direction, either $\overrightarrow{u_{E}}$ or $\overrightarrow{u_{L}}$. This assumption implies that the three dimensional effects of the light path bending are assumed to be negligible.
This simplification is quite accurate and has the advantage to allow the analytical calculation of the intersection of tangent points with such a surface.
The light path is calculated by integrating the differential Eikonal's equation in that plane:

$$
\frac{d}{d s}\left(n \frac{d}{d s} \vec{r}\right)=\nabla m
$$

where $\vec{r}$ is the position vector of a point in the light path, s is the arc length along that path, and m is the relative refraction index.

Note that iterative methods are usually needed to implement a refraction ray tracing model.

### 8.5.2.1 Standard atmosphere model

This refraction ray tracing model is based on the atmosphere model described in section 8.2.3.

### 8.5.2 2 User's atmosphere model

In this case the atmosphere model is based on a file supplied by the user, which defines the relative refraction index m at a discrete set of geometric altitudes H .

To have a continuous, and differentiable, relationship between the relative refraction index and the geometric altitude, the relative refraction index at any geometric altitude will be calculated by means of a cubic spline based on the two closest pair of data supplied by the user.

### 8.5.3 Predefined refraction corrective functions model

This model also assumes that the light path lays in a plane, i.e. the reference plane defined by the satellite position vector $\overrightarrow{r_{S C}}$, and by the known light direction, either $\overrightarrow{u_{E}}$ or $\overrightarrow{u_{L}}$.
It is based on the calculation of the parameters $\mathrm{h}_{\mathrm{T}}, \mathrm{R}_{\mathrm{T}, \mathrm{g}}$, and $\mathrm{S}_{\mathrm{T}}$ of the tangent point using the no refraction ray tracing model, and the calculation of a set of refraction corrective terms by means of predefined curves that depend only on the tangent altitude $h_{T}$ and the wavelength of the light signal $\lambda$.

Code:

Those corrective terms are:

$$
\begin{aligned}
& \Delta h_{T}=f_{1}\left(h_{T}, \lambda\right) \\
& \Delta R_{T, g}=f_{2}\left(h_{T}, \lambda\right) \\
& \Delta \theta_{E}=\Delta \theta_{L}=f_{3}\left(h_{t}, \lambda\right) \\
& \Delta S_{T}=f_{4}\left(h_{T}, \lambda\right)
\end{aligned}
$$

The tangent point, corrected for the effects of the atmosphere refraction, is calculated knowing that it lays in the reference plane, that the tangent altitude is $\mathrm{h}_{\mathrm{T}}+\Delta \mathrm{h}_{\mathrm{T}}$, and that the geometric distance from the satellite to the tangent point is $R_{T, g}+\Delta R_{T, g}$
The actual length of the light path is calculated as $\mathrm{S}_{\mathrm{T}}+\Delta \mathrm{S}_{\mathrm{T}}$
The light direction at the entrance or at the exit of the atmosphere, is calculated knowing that it lays in that reference plane, and that is deviated by an angle $\Delta \theta_{\mathrm{E}}=\Delta \theta_{\mathrm{L}}$.

The great advantage of this ray tracing model is that it is relatively quite accurate and is much faster than the refraction ray tracing models as it can be calculated analytically.

Code:

## 9 UNITS

In general, the units that will be used in all the CFI software will be the SI units, except for the angle that will use the degree instead of the radian.

Table 9: Units in CFI Software

| Quantity | Unit | Symbol |
| :--- | :--- | :--- |
| Length | meter | m |
| Mass | kilogram | kg |
| Time | second | s |
| Thermodynamic temperature | kelvin | K |
| Amount of substance | mole | mol |
| Plane angle | degree | deg |
| Frequency | hertz | Hz |
| Pressure | pascal | Pa |


[^0]:    2 This is the EO CFI Standard Transport Format. Additional Transport Formats have been defined for specific missions, see [MCD_SP].
    3 These are the EO CFI Standard ASCII Formats. Additional ASCII Formats have been defined for specific missions, see [MCD_SP].

[^1]:    4 Averaged with respect to the osculating mean anomaly over $2 \pi$.

[^2]:    5 The geometric direction is defined by the straight line that connects the initial and the final point.

